# Liquid-Liquid Equilibria of the Ternary Mixtures Water + Propanoic Acid + Methyl Ethyl Ketone and Water + Propanoic Acid + Methyl Propyl Ketone 

Alberto Arce, Antonio Blanco,* Pilar Souza, and Isabel Vidal<br>Department of Chemical Engineering, University of Santiago de Compostela, E-15706 Santiago de Compostela, Spain


#### Abstract

We report mutual solubilities of water + methyl ethyl ketone and water + methyl propyl ketone at temperatures between 25 and $55^{\circ} \mathrm{C}$, and binodal curves and liquid-liquid equilibria for water + propanoic acid + methyl ethyl ketone and water + propanoic acid + methyl propyl ketone in the same temperature range. UNIQUAC equations fitted the experimental data better than NRTL equations: the average rms phase composition error was $0.2 \%$ for UNIQUAC as compared to $0.3 \%$ for NRTL, and the rms relative error in the solute distribution ratio was $5 \%$ for UNIQUAC as compared to $7.5 \%$ for NRTL.


## Introduction

With a view to evaluating the use of methyl ethyl ketone (MEK) and methyl propyl ketone (MPK) as agents for extraction of propanoic acid from aqueous solutions, we have measured solubilities and liquid-liquid equilibria of water + propanoic acid + methyl ethyl ketone at 25,35 , and $45^{\circ} \mathrm{C}$ and water + propanoic acid + methyl propyl ketone at $25,35,45$, and $55{ }^{\circ} \mathrm{C}$. NRTL and UNIQUAC parameters were obtained from the results.

## Experimental Section

Chemicals. MEK and MPK were purchased from Carlo Erba with purities better than $99.0 \%$ and $99.8 \%$, respectively, and propanoic acid was from Merck with a purity better than $99.0 \%$; these chemicals were used without further purification. Three times distilled, deionized water was obtained in our laboratory by the usual methods.
Procedure. Solubility curves were determined by the cloud-point method in a magnetically stirred cell whose temperature was both thermostated and measured with a precision of $\pm 0.1^{\circ} \mathrm{C}$. Compositions defining the ends of tie lines were determined in a similar cell with a lateral orifice closed by a septum, through which samples of the separated phases in equilibrium were withdrawn using hypodermic syringes. In each experiment the ternary mixture to be separated was stirred vigorously for 1 h and left to settle for 4 h , which previous experiments had shown to be long enough for the phases to reach equilibrium. For diagrams of both cells, see Correa et al. (1).
Phase compositions were determined with a PerkinElmer Sigma 3 gas chromatograph with thermal conductivity detection and a Perkin-Elmer Sigma 15 integrator. Separation was performed in a $6 \mathrm{ft} \times 1 / 8 \mathrm{in}$. o.d. stainless steel column packed with Chromosorb 102 80/100, with a constant $35 \mathrm{~cm}^{3} / \mathrm{min}$ flow of helium of purity $>99.998 \%$. The oven temperature was $190^{\circ} \mathrm{C}$ for water + propanoic acid + MEK, and $200^{\circ} \mathrm{C}$ for water + propanoic acid + MPK; for both mixtures the injection and detector temperatures were $240^{\circ} \mathrm{C}$ and the detector current was 65 mA . The injection volume was always $0.2 \mu \mathrm{~L}$. Calibration was carried out using ternary mixtures made up by mass to have compositions close to the solubility curve; the chromatographically measured mole fractions of the compo-

* To whom correspondence should be addressed.

Table 1. Compositions on the Binodal Curve for the System Water (1) + Propanoic Acid (2) + Methyl Ethyl Ketone (3)

| $x_{1}$ | $x_{2}$ | $x_{3}$ | $x_{1}$ | $x_{2}$ | $x_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $t=25^{\circ} \mathrm{C}$ |  |  |  |  |
| 0.922 | 0.000 | 0.078 | 0.727 | 0.048 | 0.225 |
| 0.915 | 0.004 | 0.081 | 0.616 | 0.055 | 0.329 |
| 0.906 | 0.009 | 0.085 | 0.576 | 0.053 | 0.371 |
| 0.897 | 0.013 | 0.090 | 0.537 | 0.048 | 0.415 |
| 0.886 | 0.017 | 0.097 | 0.493 | 0.042 | 0.465 |
| 0.867 | 0.023 | 0.110 | 0.465 | 0.034 | 0.501 |
| 0.818 | 0.034 | 0.148 | 0.431 | 0.026 | 0.543 |
| 0.792 | 0.038 | 0.170 | 0.418 | 0.020 | 0.562 |
| 0.766 | 0.042 | 0.192 | 0.393 | 0.014 | 0.593 |
| 0.741 | 0.047 | 0.212 | 0.342 | 0.000 | 0.658 |
|  |  |  | $t=35{ }^{\circ} \mathrm{C}$ |  |  |
| 0.934 | 0.000 | 0.066 | 0.716 | 0.053 | 0.231 |
| 0.923 | 0.005 | 0.072 | 0.651 | 0.057 | 0.292 |
| 0.909 | 0.013 | 0.078 | 0.578 | 0.055 | 0.367 |
| 0.895 | 0.017 | 0.088 | 0.535 | 0.050 | 0.415 |
| 0.874 | 0.024 | 0.102 | 0.502 | 0.042 | 0.456 |
| 0.855 | 0.029 | 0.116 | 0.466 | 0.033 | 0.501 |
| 0.839 | 0.033 | 0.128 | 0.435 | 0.025 | 0.540 |
| 0.821 | 0.036 | 0.143 | 0.403 | 0.016 | 0.581 |
| 0.808 | 0.039 | 0.153 | 0.378 | 0.009 | 0.613 |
| 0.798 | 0.041 | 0.161 | 0.353 | 0.000 | 0.647 |
|  | $+\quad t=45$ |  |  |  | ${ }^{\circ} \mathrm{C}$ |
| 0.939 | 0.000 | 0.061 | 0.707 | 0.057 | 0.236 |
| 0.928 | 0.007 | 0.065 | 0.658 | 0.059 | 0.283 |
| 0.914 | 0.013 | 0.073 | 0.567 | 0.054 | 0.379 |
| 0.900 | 0.019 | 0.081 | 0.534 | 0.048 | 0.418 |
| 0.880 | 0.024 | 0.096 | 0.493 | 0.040 | 0.467 |
| 0.840 | 0.034 | 0.126 | 0.449 | 0.028 | 0.523 |
| 0.798 | 0.043 | 1.159 | 0.416 | 0.017 | 0.567 |
| 0.778 | 0.047 | 0.175 | 0.380 | 0.008 | 0.612 |
| 0.735 | 0.053 | 0.212 | 0.357 | 0.000 | 0.643 |
|  |  |  |  |  |  |

nents in control mixtures differed by less than 0.002 from their known values. All analyses were performed in duplicate, and duplicates coincided to within 0.002 in mole fraction.

## Results

Tables 1 and 2 list compositions corresponding to points on the binodal curves of the ternary mixtures studied at the working temperatures used. The points with zero propanoic acid concentration in these tables show that the solubility of the ketones in water was practically constant over the temperature range studied, while the solubility

Table 2. Compositions on the Binodal Curve for the System Water (1) + Propanoic Acid (2) + Methyl Propyl Ketone (3)

| $x_{1}$ | $x_{2}$ | $x_{3}$ | $x_{1}$ | $x_{2}$ | $x_{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $t=25^{\circ} \mathrm{C}$ |  |  |  |  |  |
| 0.987 | 0.000 | 0.013 | 0.698 | 0.170 | 0.132 |
| 0.977 | 0.010 | 0.013 | 0.652 | 0.185 | 0.163 |
| 0.968 | 0.018 | 0.014 | 0.589 | 0.198 | 0.213 |
| 0.959 | 0.027 | 0.014 | 0.542 | 0.201 | 0.257 |
| 0.946 | 0.038 | 0.016 | 0.493 | 0.198 | 0.309 |
| 0.937 | 0.045 | 0.018 | 0.467 | 0.192 | 0.341 |
| 0.928 | 0.052 | 0.020 | 0.442 | 0.186 | 0.372 |
| 0.919 | 0.058 | 0.023 | 0.392 | 0.166 | 0.442 |
| 0.904 | 0.068 | 0.028 | 0.361 | 0.149 | 0.490 |
| 0.889 | 0.077 | 0.034 | 0.313 | 0.128 | 0.559 |
| 0.872 | 0.087 | 0.041 | 0.275 | 0.106 | 0.619 |
| 0.844 | 0.102 | 0.054 | 0.240 | 0.086 | 0.674 |
| 0.815 | 0.117 | 0.068 | 0.182 | 0.054 | 0.764 |
| 0.770 | 0.139 | 0.091 | 0.154 | 0.032 | 0.814 |
| 0.727 | 0.158 | 0.155 | 0.140 | 0.000 | 0.860 |
| $t=35^{\circ} \mathrm{C}$ |  |  |  |  |  |
| 0.989 | 0.000 | 0.011 | 0.718 | 0.158 | 0.124 |
| 0.982 | 0.006 | 0.012 | 0.632 | 0.186 | 0.182 |
| 0.977 | 0.011 | 0.012 | 0.575 | 0.194 | 0.231 |
| 0.971 | 0.016 | 0.013 | 0.528 | 0.193 | 0.279 |
| 0.963 | 0.024 | 0.013 | 0.448 | 0.175 | 0.377 |
| 0.956 | 0.030 | 0.014 | 0.427 | 0.166 | 0.407 |
| 0.948 | 0.037 | 0.015 | 0.401 | 0.154 | 0.445 |
| 0.936 | 0.047 | 0.017 | 0.367 | 0.137 | 0.496 |
| 0.916 | 0.063 | 0.021 | 0.303 | 0.110 | 0.587 |
| 0.883 | 0.079 | 0.038 | 0.273 | 0.091 | 0.636 |
| 0.853 | 0.095 | 0.052 | 0.241 | 0.075 | 0.684 |
| 0.822 | 0.111 | 0.067 | 0.213 | 0.058 | 0.729 |
| 0.803 | 0.121 | 0.076 | 0.166 | 0.023 | 0.849 |
| 0.758 | 0.142 | 0.100 | 0.151 | 0.000 | 0.842 |
| $t=45^{\circ} \mathrm{C}$ |  |  |  |  |  |
| 0.990 | 0.000 | 0.010 | 0.721 | 0.154 | 0.125 |
| 0.982 | 0.007 | 0.011 | 0.760 | 0.172 | 0.168 |
| 0.978 | 0.011 | 0.011 | 0.624 | 0.180 | 0.196 |
| 0.972 | 0.017 | 0.011 | 0.561 | 0.184 | 0.255 |
| 0.961 | 0.026 | 0.013 | 0.532 | 0.182 | 0.286 |
| 0.953 | 0.032 | 0.015 | 0.499 | 0.176 | 0.325 |
| 0.945 | 0.039 | 0.016 | 0.471 | 0.164 | 0.363 |
| 0.932 | 0.048 | 0.020 | 0.440 | 0.153 | 0.407 |
| 0.911 | 0.062 | 0.027 | 0.378 | 0.127 | 0.495 |
| 0.876 | 0.082 | 0.042 | 0.344 | 0.113 | 0.543 |
| 0.858 | 0.091 | 0.051 | 0.314 | 0.097 | 0.589 |
| 0.822 | 0.110 | 0.068 | 0.282 | 0.080 | 0.638 |
| 0.785 | 0.127 | 0.088 | 0.213 | 0.028 | 0.759 |
| 0.749 | 0.143 | 0.108 | 0.180 | 0.000 | 0.820 |
| $t=55^{\circ} \mathrm{C}$ |  |  |  |  |  |
| 0.990 | 0.000 | 0.010 | 0.775 | 0.127 | 0.098 |
| 0.980 | 0.009 | 0.011 | 0.729 | 0.146 | 0.125 |
| 0.974 | 0.014 | 0.012 | 0.641 | 0.173 | 0.186 |
| 0.965 | 0.021 | 0.014 | 0.569 | 0.179 | 0.252 |
| 0.959 | 0.027 | 0.014 | 0.525 | 0.178 | 0.297 |
| 0.950 | 0.033 | 0.017 | 0.483 | 0.167 | 0.350 |
| 0.940 | 0.041 | 0.019 | 0.438 | 0.156 | 0.406 |
| 0.929 | 0.048 | 0.023 | 0.395 | 0.144 | 0.461 |
| 0.916 | 0.056 | 0.028 | 0.360 | 0.130 | 0.510 |
| 0.900 | 0.066 | 0.034 | 0.324 | 0.112 | 0.564 |
| 0.884 | 0.075 | 0.041 | 0.279 | 0.090 | 0.631 |
| 0.866 | 0.084 | 0.050 | 0.253 | 0.061 | 0.686 |
| 0.849 | 0.093 | 0.058 | 0.220 | 0.031 | 0.749 |
| 0.812 | 0.111 | 0.077 | 0.211 | 0.000 | 0.789 |

of water in the ketones (MPK especially) increased with temperature. These solubility results are fairly close to previously published values ( $2-10$ ) (within $0.7-10 \%$ for the temperatures used in our work) except for those reported by Siegelman and Sorum (7) for the organic phase of water + MEK mixtures, which differ by up to $21 \%$ from the corresponding findings of all other researchers. The compositions of the ends of tie lines are listed in Tables 3 and 4.

Table 3. Tie Lines for Liquid-Liquid Equilibria for Water (1) + Propanoic Acid (2) + Methyl Ethyl Ketone (3)

|  | organic phase |  |  | aqueous phase |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $t /{ }^{\circ} \mathrm{C}$ | $x_{1}$ | $x_{2}$ |  | $x_{1}$ | $x_{2}$ |
| 25 | 0.416 | 0.017 |  | 0.915 | 0.004 |
|  | 0.461 | 0.033 |  | 0.912 | 0.007 |
|  | 0.524 | 0.047 |  | 0.903 | 0.010 |
|  | 0.586 | 0.054 |  | 0.889 | 0.017 |
| 35 | 0.402 | 0.016 |  | 0.929 | 0.003 |
|  | 0.436 | 0.028 |  | 0.928 | 0.005 |
|  | 0.484 | 0.040 |  | 0.919 | 0.008 |
|  | 0.517 | 0.051 |  | 0.912 | 0.011 |
|  | 0.563 | 0.055 |  | 0.905 | 0.015 |
| 45 | 0.618 | 0.057 |  | 0.894 | 0.019 |
|  | 0.418 | 0.019 |  | 0.933 | 0.004 |
|  | 0.458 | 0.033 |  | 0.930 | 0.006 |
|  | 0.505 | 0.047 |  | 0.923 | 0.010 |
|  | 0.567 | 0.055 |  | 0.912 | 0.014 |
|  | 0.618 | 0.059 |  | 0.902 | 0.018 |

Table 4. Tie Lines for Liquid-Liquid Equilibria for Water (1) + Propanoic Acid (2) + Methyl Propyl Ketone (3)

|  | organic phase |  |  | aqueous phase |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $t /{ }^{\circ} \mathrm{C}$ | $x_{1}$ | $x_{2}$ |  | $x_{1}$ | $x_{2}$ |
| 25 | 0.238 | 0.061 | 0.980 | 0.006 |  |
|  | 0.335 | 0.134 | 0.974 | 0.013 |  |
|  | 0.420 | 0.182 | 0.964 | 0.023 |  |
|  | 0.499 | 0.201 | 0.952 | 0.033 |  |
|  | 0.583 | 0.202 | 0.938 | 0.046 |  |
|  | 0.746 | 0.151 | 0.887 | 0.079 |  |
| 35 | 0.258 | 0.083 | 0.985 | 0.007 |  |
|  | 0.359 | 0.139 | 0.976 | 0.014 |  |
|  | 0.460 | 0.167 | 0.963 | 0.023 |  |
|  | 0.519 | 0.187 | 0.953 | 0.031 |  |
|  | 0.599 | 0.192 | 0.935 | 0.046 |  |
| 45 | 0.715 | 0.161 | 0.906 | 0.067 |  |
|  | 0.262 | 0.065 | 0.982 | 0.006 |  |
|  | 0.360 | 0.133 | 0.974 | 0.014 |  |
|  | 0.495 | 0.165 | 0.963 | 0.024 |  |
|  | 0.528 | 0.180 | 0.955 | 0.031 |  |
|  | 0.627 | 0.182 | 0.933 | 0.048 |  |
| 55 | 0.743 | 0.144 | 0.906 | 0.067 |  |
|  | 0.247 | 0.065 | 0.983 | 0.006 |  |
|  | 0.306 | 0.108 | 0.981 | 0.010 |  |
|  | 0.362 | 0.134 | 0.974 | 0.014 |  |
|  | 0.408 | 0.146 | 0.970 | 0.017 |  |
|  | 0.460 | 0.167 | 0.962 | 0.024 |  |
|  | 0.540 | 0.178 | 0.954 | 0.032 |  |
|  | 0.566 | 0.184 | 0.945 | 0.037 |  |
|  | 0.641 | 0.174 | 0.933 | 0.047 |  |

## Data Correlation

The NRTL (11) and UNIQUAC (12) models (see Appendix) were fitted to the experimental data for each system and temperature using Sørensen's (13-15) computer program. The NRTL equations were obtained for three prefixed values of the nonrandomness parameter $\alpha_{i j}: 0.1,0.2$, and 0.3 . Optimizable parameters were found by minimizing the objective function

$$
\begin{equation*}
F_{x}=\sum^{k} \sum^{i} \sum^{j}\left(x_{i j k}-\hat{x}_{i j k}\right)^{2}+Q \sum^{n} P_{n}{ }^{2}+\left[\ln \left(\frac{\hat{\gamma}_{\mathrm{S}_{\infty}}^{\mathrm{I}}}{\hat{\gamma}_{\mathrm{S}_{\infty}}^{\mathrm{II}}} \beta_{\infty}\right)\right]^{2} \tag{1}
\end{equation*}
$$

with or without the last term. In this equation, $x_{i j k}$ and $\hat{x}_{i j k}$ are, respectively, the observed and calculated mole fractions of component $i$ in phase $j$ on tie line $k$, the second term on the right-hand side is a penalty term to reduce the risk of multiple solutions ( $P_{n}=a_{i j}$ for the NRTL equation and $b_{i j}$ for the UNIQUAC equation; $Q$ is set to $10^{-10}$ ), and the third term, in which $\beta_{\infty}$ is the solute distribution ratio at infinite dilution and $\hat{\gamma}_{S_{n}}^{X}$ is the calcu-

Table 5. Values of the Goodness-of-Fit Evaluators $F$ and $\Delta \beta$ (Eqs 2 and 3) Achieved in Fitting UNIQUAC and NRTL Equations to the Experimental Data for Water + Propanoic Acid + Methyl Ethyl Ketone

| model |  | $t=25^{\circ} \mathrm{C}$ |  | $t=35^{\circ} \mathrm{C}$ |  | $t=45^{\circ} \mathrm{C}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| UNIQUAC | $\beta_{\infty}$ |  | 5.9 |  | 6.3 |  | 6.7 |
|  | $F(\%)$ | 0.10 | 0.11 | 0.12 | 0.12 | 0.10 | 0.10 |
|  | $\Delta \beta$ (\%) | 10.80 | 7.6 | 7.8 | 7.4 | 5.1 | 4.9 |
| NRTL$\left(\alpha_{i j}=0.1\right)$ | $\beta_{\infty}$ |  | 7.4 |  | 7.7 |  | 7.7 |
|  | $F(\%)$ | 0.17 | 0.22 | 0.23 | 0.25 | 0.21 | 0.24 |
|  | $\Delta \beta$ (\%) | 16.1 | 12.1 | 14.9 | 12.2 | 14.9 | 8.2 |
| NRTL$\left(\alpha_{i j}=0.2\right)$ | $\beta_{\infty}$ |  | 6.7 |  | 8.7 |  | 10.1 |
|  | $F(\%)$ | 0.11 | 0.20 | 0.19 | 0.30 | 0.15 | 0.31 |
|  | $\Delta \beta$ (\%) | 25.6 | 10.8 | 24.1 | 14.3 | 24.4 | 12.5 |
| NRTL$\left(\alpha_{i j}=0.3\right)$ | $\beta_{\infty}$ |  | 8.1 |  | 8.6 |  | 9.4 |
|  | $F(\%)$ | 0.08 | 0.03 | 0.16 | 0.28 | 0.12 | 0.28 |
|  | $\Delta \beta$ (\%) | 26.9 | 14.0 | 24.0 | 13.7 | 23.7 | 11. |

Table 6. Values of the Goodness-of-Fit Evaluators $F$ and $\Delta \beta$ (Eqs 2 and 3) Achieved in Fitting UNIQUAC and NRTL Equations to the Experimental Data for Water + Propanoic Acid + Methyl Propyl Ketone

| model |  | $t=25^{\circ} \mathrm{C}$ |  | $t=35^{\circ} \mathrm{C}$ |  | $t=45^{\circ} \mathrm{C}$ |  | $t=55^{\circ} \mathrm{C}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| UNIQUAC | $\beta_{\infty}$ |  | 12.6 |  | 14.7 |  | 12.1 |  | 13.0 |
|  | $F(\%)$ | 0.35 | 0.35 | 0.26 | 0.27 | 0.31 | 0.32 | 0.13 | 0.14 |
|  | $\Delta \beta$ (\%) | 6.5 | 6.4 | 5.7 | 3.4 | 4.9 | 4.6 | 1.6 | 1.3 |
| NRTL$\left(\alpha_{i j}=0.1\right)$ | $\beta_{\infty}$ |  | 9.7 |  | 11.5 |  | 9.7 |  | 2.2 |
|  | $F(\%)$ | 1.12 | 0.46 | 0.92 | 1.62 | 0.97 | 1.75 | 0.69 | 1.28 |
|  | $\Delta \beta$ (\%) | 16.1 | 6.8 | 40.3 | 12.1 | 60.7 | 18.6 | 48.8 | 7.6 |
| NRTL$\left(\alpha_{i j}=0.2\right)$ | $\beta_{\infty}$ |  | 13.3 |  | 16.5 |  | 12.8 |  | 12.8 |
|  | $F(\%)$ | 0.50 | 0.51 | 0.31 | 0.31 | 0.41 | 0.42 | 0.20 | 0.20 |
|  | $\Delta \beta$ (\%) | 18.6 | 8.6 | 5.1 | 4.0 | 10.4 | 6.4 | 3.3 | 1.8 |
| NRTL$\left(\alpha_{i j}=0.3\right)$ | $\beta_{\infty}$ |  | 12.3 |  | 16.0 |  | 11.7 |  | 13.1 |
|  | $F(\%)$ | 0.62 | 0.64 | 0.35 | 0.35 | 0.50 | 0.50 | 0.24 | 0.25 |
|  | $\Delta \beta$ (\% | 49.5 | 9.6 | 9.1 | 4.8 | 15.0 | 7.2 | 11.3 | 2.5 |

lated activity coefficient of the solute at infinite dilution in phase $X$, accentuates deviation between the experimental and calculated results in the low solute concentration region.
Two a posteriori goodness-of-fit criteria were calculated: the rms error in mole fractions,

$$
\begin{equation*}
F=100\left[\sum^{k} \sum^{i} \sum^{j}\left(x_{i j k}-\hat{x}_{i j k}\right)^{2} / 6 M\right]^{1 / 2} \tag{2}
\end{equation*}
$$

where $M$ is the number of tie lines, and the rms relative error in the solute distribution ratio,

$$
\begin{equation*}
\Delta \beta=100\left[\sum^{k}\left[\frac{\hat{\beta}_{k}-\beta_{k}}{\beta_{k}}\right]^{2} / M\right]^{1 / 2} \tag{3}
\end{equation*}
$$

where $\beta_{k}$ and $\hat{\beta}_{k}$ are, respectively, the experimental and calculated solute distribution ratios for tie line $k$.
When the $\beta_{\infty}$ term was included in the objective function, the optimal value of $\beta_{\infty}$ was identified by trial and error ("manually" optimized) as the value minimizing $\Delta \beta$.
Tables 5 and 6 list the values of $F$ and $\Delta \beta$ of the curves fitted to the experimental data for each mixture and temperature. For curves optimized with the $\beta_{\infty}$ term included in the objective function, the manually optimized value of $\beta_{\infty}$ is also shown. Including the $\beta_{\infty}$ term is generally preferable for these data, since the composition error $F$ is increased only slightly overall, while the improvement in $\Delta \beta$ is considerable, especially for the NRTL model (and is moreover due largely to reduction of $\mid \hat{\beta}_{k}-$ $\beta_{k} \mid$ in the low solute concentration region, which is of particular interest for separation operations). The UNIQUAC equation generally fitted better, especially in terms of $\Delta \beta$, than the NRTL equation (with which best results were achieved with $\alpha_{i j}=0.1$ for the MEK mixture and $\alpha_{i j}$

Table 7. Values of the Parameters of the NRTL
Equations Fitted to the Experimental Data for Water (1) + Propanoic Acid (2) + Methyl Ethyl Ketone (3)

| $t /{ }^{\circ} \mathrm{C}$ | $\beta_{\infty}$ | $\alpha_{i j}$ | $i-j$ | $a_{i j}{ }^{a} / \mathrm{K}$ | $a_{j i} / \mathrm{K}$ |
| :---: | :---: | :---: | :---: | ---: | ---: |
| 25 | 7.4 | 0.1 | $1-2$ | -896.40 | -114.30 |
|  |  |  | $1-3$ | 1330.60 | -387.83 |
| 35 | 7.7 | 0.1 | $2-3$ | -1332.80 | 768.35 |
|  |  |  | $1-3$ | -1028.10 | -200.71 |
|  |  | 1436.20 | -421.33 |  |  |
| 45 | 7.7 | 0.1 | $2-3$ | $-1-2$ | -1041.30 |
|  |  |  | $1-3$ | 1537.80 | -5.59 |
|  |  |  | $2-3$ | -1400.60 | -468.39 |
|  |  |  |  |  | 1035.80 |

${ }^{a} a_{i j}=\left(g_{i j}-g_{j j}\right) / R$.
Table 8. Values of the Parameters of the NRTL
Equations Fitted to the Experimental Data for Water (1)

+ Propanoic Acid (2) + Methyl Propyl Ketone (3)

| $t /{ }^{\circ} \mathrm{C}$ | $\beta_{\infty}$ | $\alpha_{i j}$ | $i-j$ | $a_{i j}{ }^{6 / K}$ | $a_{j i} / \mathrm{K}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 25 | 13.3 | 0.2 | 1-2 | 1484.50 | -657.54 |
|  |  |  | 1-3 | 1204.10 | 117.57 |
|  |  |  | 2-3 | -524.73 | 535.34 |
| 35 | 16.5 | 0.2 | 1-2 | 1570.18 | -757.18 |
|  |  |  | 1-3 | 1269.80 | 138.60 |
|  |  |  | 2-3 | -374.70 | 72.29 |
| 45 | 12.8 | 0.2 | 1-2 | 1686.80 | -790.66 |
|  |  |  | 1-3 | 1329.70 | 111.06 |
|  |  |  | 2-3 | -355.17 | 137.27 |
| 55 | 12.8 | 0.2 | 1-2 | 1603.50 | -800.63 |
|  |  |  | 1-3 | 1382.30 | 132.14 |
|  |  |  | 2-3 | -64.25 | --322.80 |

Table 9. Values of the Parameters of the UNIQUAC
Equations Fitted to the Experimental Data for Water (1) + Propanoic Acid (2) + Methyl Ethyl Ketone (3)

| $t /{ }^{\circ} \mathrm{C}$ | $\beta_{\infty}$ | $i-j$ | $b_{i j} a / \mathrm{K}$ | $b_{j i} / \mathrm{K}$ |
| :---: | :---: | :---: | ---: | ---: |
| 25 | 5.9 | $1-2$ | 120.14 | -142.34 |
|  |  | $1-3$ | 1.48 | 328.64 |
|  |  | $2-3$ | 91.94 | -145.14 |
| 35 | 6.3 | $1-2$ | 209.14 | -155.44 |
|  |  | $1-3$ | 20.70 | 309.36 |
|  |  | $2-3$ | 192.44 | -248.92 |
| 45 | 6.7 | $1-2$ | 224.67 | -207.78 |
|  |  | $1-3$ | 35.09 | 296.15 |
|  |  | $2-3$ | 87.45 | -249.39 |

$$
{ }^{a} b_{i j}=\left(u_{i j}-u_{j j}\right) / R .
$$

Table 10. Values of the Parameters of the UNIQUAC Equations Fitted to the Experimental Data for Water (1) + Propanoic Acid (2) + Methyl Propyl Ketone (3)

| $t /{ }^{\circ} \mathrm{C}$ | $\beta_{\infty}$ | $i-j$ | $b_{i j}{ }^{a} / \mathrm{K}$ | $b_{j /} / \mathrm{K}$ |
| :---: | :---: | :---: | ---: | ---: |
| 25 | 12.6 | $1-2$ | 14.32 | -82.63 |
|  |  | $1-3$ | 114.63 | 301.47 |
| 35 | 14.7 | $2-3$ | 745.91 | -488.84 |
|  |  | $1-2$ | 348.32 | -210.14 |
|  |  | $1-3$ | 93.12 | 381.32 |
| 45 | 12.1 | $2-3$ | 31.52 | -110.86 |
|  |  | $1-2$ | 201.50 | -169.36 |
|  |  | $1-3$ | 132.16 | 309.51 |
| 55 | 13.0 | $2-3$ | 375.90 | -110.86 |
|  |  | $1-2$ | 242.72 | -182.56 |
|  |  | $1-3$ | 101.85 | 377.04 |
|  |  | $2-3$ | 211.18 | -289.25 |
| ${ }^{3} b_{i j}=\left(u_{i j}-u_{j j}\right) / R$. |  |  |  |  |
|  |  |  |  |  |

$=0.2$ for the MPK mixture); Tables $7-10$ list the optimized NRTL and UNIQUAC parameters, and Figures 1 and 2 show, for each ternary mixture and temperature, the experimental equilibrium data and the corresponding optimized UNIQUAC and NRTL curves.


Figure 1. 1. Liquid--liquid equilibrium data for water (1) + propanoic acid (2) + methyl ethyl ketone (3) at 25,35 , and $45^{\circ} \mathrm{C}$ : experimental equilibrium phase compositions ( O ) and calculated binodal curves and tie lines obtained by fitting UNIQUAC ( - ) and NRTL ( $\ldots$ ) equations (the latter with $\alpha_{i j}=0.1$ ).

## Conclusions

The experimentally determined liquid-liquid equilibria of the binary mixtures water + methyl ethyl ketone at temperatures of 25,35 , and $45^{\circ} \mathrm{C}$ and water + methyl propyl ketone at temperatures of $25,35,45$, and $55^{\circ} \mathrm{C}$ show that in these temperature ranges the solubility of the ketone in water is practically independent of temperature, while the solubility of water in the ketones increases slightly with temperature.

Solubility and liquid-liquid equilibrium data were also determined experimentally for the ternary mixtures water + propanoic acid + methyl ethyl ketone at temperatures of 25,35 , and $45^{\circ} \mathrm{C}$ and water + propanoic acid + methyl propyl ketone at temperatures of $25,35,45$, and $55{ }^{\circ} \mathrm{C}$. Fitting NRTL and UNIQUAC equations to the experimental liquid-liquid equilibrium data showed that, in general, the best fit was given by the UNIQUAC model.

In view of the high ratios between the concentrations of propanoic acid in the organic and the aqueous phases of these systems, both ketones are suitable for extraction of propanoic acid from aqueous solutions (though the use of MEK would be limited to very dilute solutions). The
immiscible region is considerably greater with MPK than with MEK. In the range of temperature considered, this variable has practically no effect on either the size of the immiscible region or the slopes of tie lines.

## Appendix: NRTL and UNIQUAC Equations

In both the following definitions, $R$ is the universal gas constant ( $\mathrm{J} /(\mathrm{mol} \cdot \mathrm{K})$ ), $T$ is temperature ( K ), $G^{\mathrm{E} / R T}$ is the dimensionless excess Gibbs energy of a mixture of $n$ components indexed by subscripts $i$ and $j$, and $x_{i}$ is the mole fraction of component $i$.

## NRTL Equation

$$
\begin{gathered}
\frac{G^{\mathrm{E}}}{R T}=\sum_{i} x_{i} \frac{\sum_{j} \tau_{j i} G_{j i} x_{j}}{\sum_{j} G_{j i} x_{j}} \\
i, j=1,2, \ldots, n \text { (components) }
\end{gathered}
$$

where $\tau_{i j}$ is given by

$$
\tau_{j i}=\frac{g_{j i}-g_{i i}}{R T}
$$

( $g_{i j}$ being a parameter characterizing the energy of interaction between components $i$ and $j ; g_{j i}=g_{i j}$ ) and $G_{j i}$ is given by

$$
G_{j i}=\exp \left(-\alpha_{j i} \tau_{j i}\right)
$$

( $\alpha_{j i}$ being related to the degree of nonrandomness of the mixture; $\alpha_{j i}=\alpha_{i j}$ ). The NRTL equation is fitted to composition data by optimizing the parameters $a_{i j}=T \tau_{j i}$.

UNIQUAC Equation

$$
\begin{gathered}
\frac{G^{\mathrm{E}}}{R T}=\sum_{i} x_{i} \ln \frac{\phi_{i}}{X_{i}}+5 \sum_{i} Q_{i} x_{i} \ln \frac{\theta_{i}}{\phi_{i}}-\sum_{i} Q_{i} x_{i} \ln \left[\sum_{j} \theta_{j} \tau_{j i}\right] \\
i, j=1,2, \ldots, n \text { (components) }
\end{gathered}
$$

where $\tau_{i j}$ is given by

$$
\tau_{j i}=\exp \left(-\frac{u_{j i}-u_{i i}}{R T}\right)
$$

( $u_{i j}$ being a parameter characterizing the energy of interaction between components $i$ and $j ; u_{i j}=u_{j i}$ ) and $\phi_{i}$ and $\theta_{i}$ are given by

$$
\phi_{i}=\frac{x_{i} R_{i}}{\sum_{j} x_{j} R_{j}} \quad \theta_{i}=\frac{x_{i} Q_{i}}{\sum_{j} x_{j} Q_{j}}
$$

(the $R_{i}$ and $Q_{i}$ being parameters characterizing, respectively, the molecular volume and molecular surface area of pure component $i$ ). The UNIQUAC equation is fitted to composition data by optimizing the parameters $b_{i j}=\left(u_{i j}\right.$ - $\left.u_{j j}\right) / R$. For this work, the values of the structural parameters $R_{i}$ and $Q_{i}$ were taken from ref 16: $R_{\mathrm{H}_{2} \mathrm{O}}=0.92$, $Q_{\mathrm{H}_{2} \mathrm{O}}=1.40 ; R_{\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{COOH}}=2.8768, Q_{\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{COOH}}=2.612 ; R_{\mathrm{MEK}}$ $=3.2479, Q_{\mathrm{MEK}}=2.876 ; R_{\mathrm{MPK}}=3.9223, Q_{\mathrm{MPK}}=3.416$.


Figure 2. 2. Liquid-liquid equilibrium data for water (1) + propanoic acid (2) + methyl propyl ketone (3) at $25,35,45$, and $55^{\circ} \mathrm{C}$ experimental equilibrium phase compositions $(O)$ and calculated binodal curves and tielines obtained by fitting UNIQUAC $(-)$ and NRTL ( $\cdots$ ) equations (the latter with $\alpha_{i j}=0.2$ ).

## Literature Cited

(1) Correa, J. M.; Blanco, A.; Arce, A. J. Chem. Eng. Data 1989, 34 (4), 415 .
(2) Evans, T. W. Ind. Eng, Chem. 1936, 8, 206.
(3) Ginnings, P. M.; Plonk, D.; Carter, E. J. J. Am. Chem. Soc. 1940, 62, 1923.
(4) Newman, M.; Hayworth, C. B.; Treybal, R. E. Ind. Eng. Chem. 1949, 41, 2039.
(5) Regna, E. A.; Bruins, P. F. Ind. Eng. Chem. 1956, 48, 1268.
(6) Campbell, A. N.; Kartzmark, E. M.; Falconer, W. E. Can. J. Chem. 1958, 35, 1475.
(7) Siegelman, I.; Sorum, C. H. Can. J. Chem. 1960, 38, 2015.
(8) Iguchi, A.; Fuse, K. Kagaku Kogaku 1971, 35, 477.
(9) Gross, P. M.; Rintelen, J. C.; Saylor, J. M. J. Phys. Chem. 1939, $43,197$.
(10) Sørensen, J. M.; Arlt, W. Liquid-liquid equilibrium Data Collection. Binary Systems; DECHEMA Data Series; DECHEMA: Frankfurt, 1979; Vol. V, Part 1.
(11) Renon, H.; Prausnitz, J. M. AIChE J. 1968, 14, 135.
(12) Abrams, D. S.; Prausnitz, J. M. AIChE J. 1975, 21, 116.
(13) Sørensen, J. M; Magnussen, T.; Rasmussen, P.; Fredenslund, Aa Fluid Phase Equilib. 1979, 3, 47.
(14) Magnussen, T.; Sørensen, J. M; Rasmussen, P.; Fredenslund, Aa. Fluid Phase Equilib. 1980, 4, 151.
(15) Sørensen, J. M. Correlation of Liquid-liquid Equilibrium Data. Ph.D. Thesis, Technical University of Denmark, Lingby, Denmark, 1980.
(16) Magnussen, T.; Rasmussen, P.; Fredenslund, Aa. Ind. Eng. Chem. Process Des. Dev. 1981, 20, 331.

Received for review June 3, 1994. Accepted September 28, $1994{ }^{\otimes}$ JE940104N

[^0]
[^0]:    * Abstract published in Advance ACS Abstracts, December 1, 1994.

